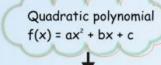
+ BOARD, NDA, FOUNDATION



Relationship b/w zeros & coefficients

Sum of zeros =
$$\frac{-\text{coefficient of x}}{\text{coefficient of x}^2} - \frac{b}{a}$$

Product of zeros =
$$\frac{\text{constant term}}{\text{coefficient of } x^{2}} = \frac{c}{a}$$

If zeros of quadratic polynomial is α and β then polynomial is f(x) = $k\{x^2 - (\alpha + \beta) \times + \alpha\beta\}$ where k is any real number.

Value of polynomial

The value of a polynomial f(x) at $x = \alpha$ is obtained by substituting $x = \alpha$ in the given polynomial and is denoted by $f(\alpha)$. e.g. If $f(x) = 2x^3-13x^2+17x+12$ then its value at x = 1 is $f(1) = 2(1)^2-13(1)^2+17(1)+12$ = 2-13+17+12=18.

Factor theorem

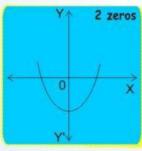
If p(x) is a polynomial and 'a' be a real number, such that p(a) = 0, then (x-a) is a factor of p(x). e.g. Factors of $f(x) = x^2 - 3x + 2$ is (x-2)(x-1)

e.g. Factors of
$$f(x) = x^2 - 3x + 2$$
 is $(x-2)(x-1)$
 $f(1) = 1^2 - 3(1) + 2 = 1 - 3 + 2 = 0$

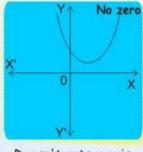
&
$$f(2) = 2^2 - 3(2) + 2 = 4 - 6 + 2 = 0$$

Polynomials

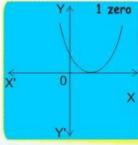
An algebraic expression f(x) of the form $f(x) = a_0 + a_1x + a_2x^2 + \dots + a_nx^n$, where $a_0, a_1, a_2, \dots, a_n$ are real numbers and all the index of x are non-negative integers is called polynomials in x and the highest Index n is called the degree of the polynomial.



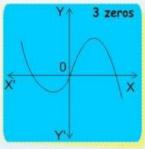
It cuts x axis twice.



Doesn't cuts x axis.



It touches x axis.



It cuts x axis 3 times.

Division Algorithm

Dividend = Divisior × Quotient + Remainder

OR

$$f(x) = g(x) \times q(x) + r(x)$$

Degree of
$$q(x) = \deg_{x} f(x) - \deg_{x} g(x)$$

Degree of
$$r(x) < deg. g(x)$$

Cubic polynomial $f(x) = ax^3 + bx^2 + cx + d$

Relationship b/w zeros & coefficients

Sum of zeros =
$$\frac{-\text{coefficient of } x^2}{\text{coefficient of } x^3} = -\frac{b}{a}$$

Product of zeroes =
$$\frac{-\text{constant term}}{\text{coefficient of } x^2} = \frac{-d}{a}$$

If zeros of cubic polynomial is
$$\alpha,\,\beta\,$$
 and γ then polynomial is

$$f(x) = k\{x^3 - (\alpha + \beta + \gamma) \times + (\alpha\beta + \beta\gamma + \gamma\alpha)x - \alpha\beta\gamma\}$$

where k is any real number.

Remainder theorem

If f(x) is a polynomial and 'a' be a real number, then if f(x) is divided by (x-a), then the remainder is equal to f(a). e.g Find the remainder when $f(x) = x^3 + 6x^2 - 3x + 5$ is divided by g(x) = x + 2. Sol. x + 2 = 0 $\Rightarrow x = -2$ Remainder = f(-2)= $(-2)^3 + 6(-2)^2 - 3(-2) + 5$ = -8 + 24 + 6 + 5= 27

NCERT / X / Polynomial



